A singular Cauchy problem for a system of implicit Volterra integro-differential equations is considered. With the aid of Banach contraction principle, the theorem concerning the existence and uniqueness of a solution of this problem (having the graph in a prescribed domain) is proved. Moreover, continuous dependence of a solution on a parameter is investigated as well.